Original Article

Comparative Analysis of Panel Data Regression Models on Nigeria Money Deposit Bank Dataset

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Abstract - Panel data regression models have gained significant attention in empirical research due to their ability to capture both cross-sectional and time-series variations. This study conducts a comparative analysis of panel data regression models using a dataset from Nigeria's Money Deposit Banks. The research focuses on examining the performance of these models in estimating the relationship between key financial indicators and bank profitability. The dataset spans from 2001 to 2020, providing a comprehensive view of the banks' financial status using the Return on Asset (RoA). The study employs two-panel data regression models: Fixed Effects and Random Effects models. The models are compared based on their goodness-of-fit metrics' values, as measured by the Adjusted R-squared, F-statistic, Log-likelihood and AIC. The study also considers the significance and direction of the coefficients of the independent variables. Preliminary results suggest that the Fixed Effects model with 0.71, 9.66, 97.15, and -148.3 values for Adjusted R-squared, F-statistic, Log-likelihood and AIC metrics, respectively.

Keywords - Panel data regression models, Bank profitability, Nigeria money deposit banks, Comparative analysis, Fixed effects model.

1. Introduction

Panel data regression models have become vital tools in empirical research, notably in economics and finance, since they can handle both cross-sectional and time-series changes at the same time [1]. In banking research, these models provide strong analytical frameworks for evaluating numerous aspects of bank performance, such as profitability, risk management, and regulatory compliance [2]. With Nigeria's banking system rapidly evolving in the face of dynamic market circumstances and regulatory changes, stakeholders must grasp the factors that influence Money Deposit Bank (MDB) performance [3].

Existing research on the Nigerian banking industry frequently uses traditional time series or cross-sectional analysis, which may not completely capture the dynamic interactions between variables. Studies using panel data for the Nigerian banking industry may focus on certain models without thoroughly assessing the performance of various models. This study fills a knowledge gap by comparing twopanel data regression models used on a panel dataset of Nigerian money deposit institutions. The study assesses the merits and shortcomings of two distinct models for describing the links between major variables impacting Nigeria's banking system. Despite the proliferation of research using panel data regression in money deposit banks, detailed comparison analyses are required to determine the best appropriate modelling method between the Random effects and Fixed effects models in the Nigerian Money Deposit Banks setting. This study is an extract from a PhD thesis, which validates the intention of the researcher in the adoption of panel data regression models. Therefore, the data preprocessing algorithm analysis is not within the scope of this paper.

The purpose of this study is to compare the empirical outputs of the Random effects and Fixed effects models using the Hausman test to determine their certainty. To achieve this goal, the panel dataset from ten Nigerian money deposit banks was studied using a dataset spanning 2001 to 2020, offering a full assessment of the institutions' financial situation.

2. Panel Data Description

Repeated data collection from the same population necessitates a cross-sectional examination of the influence of factor variables on outcome variables. Panel data analysis arose as a result of the advancement of econometric modelling approaches, sophisticated statistical methodologies, and computer data processing technologies [4]. The first uses of this sort of data may be found in longitudinal research on societal problems [5]. The increased interest in understanding macroeconomic events, as well as the great availability of data for specific samples, have significantly contributed to the continued use of panel data analysis in the study of macroeconomic indicator dynamics. Assessing an organization's performance, particularly in the banking sector, is critical to shareholder decision-making because shareholders base their decisions to invest available cash in the assets of the firm on performance criteria [6].

The return on equity is reflected in the assessment of corporate performance based on the degree of shareholder equity [7]. Return on Equity (ROE) varies from one organization to organization; it varies from one financial record to another within the same organization, and to be able to determine such dynamics require the use of panel data to assess over time the effects of determinant factors on return on equity.

2.1. Conceptual Model of Panel Data

The conceptual model of panel data describes the methodology flow used in panel data analysis. Figure 1 shows a diagrammatic representation of the existing general framework used for panel data analysis, which was suggested and used in [8].



Fig. 1 Panel data analysis conceptual framework [8]

2.2. Groundwork for Panel Data

The panel data are sometimes referred to as pooled data or longitudinal data. A panel dataset is a collection of crosssection data Y_{nt} (n = 1, ..., N and t = 1, ..., T) produced from statistical observation of characteristics typical of a group of N persons done on a regular basis during a defined time interval T [9]. A panel dataset has a variation in observations for the same persons throughout time, resulting in the recording of N.T observations. According to this representation, statistical observations exhibit a variety of individual traits, which contributes to an increase in the variability of observations and accuracy of estimation.

2.3. Characteristics of Panel Data

Panel data, according to [10], is the result of many recordings of the same persons in a specified sample during a specific time period. Even if the criterion for random selection is quite stringent in the observed sample, eventually, correlations between markers describing people over time can be formed.

- A. If panel data is analyzed by the size of the sample, then;
 - i. Balanced panel data: This is obtained when an individual data point is observed over equal periods of time
 - ii. Unbalanced panel data: This is obtained when individual data points are observed over different periods of time.
- B. If panel data is analyzed by the selection methods of individual data points, then;
 - i. Continuous panel data: The chosen individuals for the sample do not vary during the recording of observations.
 - ii. Rotative panel data: When a population is observed over a set amount of time, they may be removed from the sample and replaced with other people for whom fresh observations will be collected.

The features of panel data are represented using the function in Equation (1)

$$Y_{nt}(n = 1, ..., N \text{ and } t = 1, ..., T)$$
 (1)

For statistical observation using panel data, it defines three perspectives: person N, time T, and variable Y. Y_{nt} is the observed variable Y for individual N at instant T, according to these notations. Panel data sets, as indicated in equation 1, are distinguished by their double-dimensional representation, temporal and transverse, giving them a major advantage over other forms of data.

The temporal dimension tracks an individual's progress across time in relation to the factors under consideration. This dimension specifies the statistical recording of data from each observed statistical unit as a time series. On this dimension, the breakdown of total variability in each recorded observation should take into account the number of research periods. The entire variance in this example may be broken down as shown in equations (2 - 7);

Which is represented mathematically in equation 2.6.

$$\frac{\sum_{n=1}^{N} \sum_{t=1}^{T} (y_{nt} - y_{..})^2}{y_{..})^2 + \sum_{n=1}^{N} \sum_{t=1}^{T} (y_{nt} - y_{.t})^2} = N \sum_{t=1}^{T} (y_{.t} - y_{.t})^2$$
(3)

Transversal dimension examines the variation of characteristics from one individual to another regardless of the time t during which data have been collected, and total variance can be decomposed.

Which is represented mathematically in Equation (5)

$$\sum_{n=1}^{N} \sum_{t=1}^{T} (y_{nt} - y_{..})^2 = N \sum_{n=1}^{N} (y_{n.} - y_{..})^2 + \sum_{n=1}^{N} \sum_{t=1}^{T} (y_{nt} - y_{n.})^2$$
(5)

The whole variance of recorded observations can be dissected by active combining of the two dimensions as shown in Equation (6),

Total variance = Inter – individual variance + Inter – temporal variance + Intra – individual – temporal variance (6)

The mathematical form of Equation (6) is shown in Equation (7).

$$\sum_{n=1}^{N} \sum_{t=1}^{T} (y_{nt} - y_{..})^2 = N \sum_{t=1}^{T} (y_{.t} - y_{..})^2 + T \sum_{n=1}^{N} (y_{n.} - y_{..})^2 + \sum_{n=1}^{N} \sum_{t=1}^{T} (y_{nt} - y_{n.} - y_{.t} - y_{..})^2$$
(7)

The main difference between the last breakdown and the first two is that it takes into account both intra-temporal and intra-individual variances. The fundamental advantage of investigating people's behaviour from the perspective of the person and the temporal dimensions is the breakdown technique of total variance, as in the previous model.

2.4. Panel Analysis Models

To carry out panel data analysis, a general model given in [8] is usually the starting model. This model is adjusted to suit specific panel data analysis tasks. This model is frequently built using a set of data collected for N individuals over a T-year period. Given this data, the following generic model for the analysis of a resultative variable (Y) by determinant factors (X_k) may be written as suggested in Equation (8) [8];

$$y_{nt} = b_{0nt} + \sum_{k=1}^{K} b_{knt} + x_{knt} + w_{nt}$$
(8)

n = 1, ..., N and t = 1, ..., T, where y_{nt} represents dependent variable values, x_{knt} represents independent variable values K, b_{0nt} is a constant, and w_{nt} is the error component.

 b_{0nt} and b_{knt} coefficients, k = 1, ..., K vary over time and across people. Because individuals' behaviour towards dependent variables of the researched sample may change over time, there may be a lack of recorded data homogeneity in the examined sample. It is difficult to estimate the model using standard approaches since the number of coefficients (NT(K + 1)) is more than the total number of data (NT). Contrasts between coefficients should be employed in this scenario by defining two classical models: fixed effects models (individual or temporal) and compounded error models (random effects).

2.4.1. Random Effects Model

In fixed effects models, it is believed that the influence of the investigated factor variables (x_{knt}) on the dependent variable (y_{nt}) is the same for all people across the whole studied time $(b_{knt} = b_k)$. In this scenario, the constant b_{0nt} can be decomposed as given in Equation (9);

$$b_{0nt} = b_0 + a_n + d_t (9)$$

Where, b_{0nt} is the constant of the regression model, b_0 , a constant

 a_n indicates unobservable differences between individuals and d_t temporal differences that may appear in individuals.

The regression model is given in Equation (10).

$$y_{nt} = b_0 + a_n + d_t + \sum_{k=1}^{K} b_k x_{knt} + w_{nt}$$
(10)

In estimating fixed effects model parameters, take into account individual and temporal specificity by incorporating unique effects, also known as fixed effects, in individuals and periods that indicate coefficients to be calculated. Two banks with the same observable properties should have the same values for the resultative variables in the case of a model for a certain period.

2.4.2. Fixed Effect Model

Generally, the fixed effect models are given, as shown in Equation (11). The unpredictable nature of specific effects distinguishes composite effect models from fixed effect models.

$$y_{nt} = b_{0nt} + \sum_{k=1}^{K} b_k x_{knt} + \varepsilon_{nt}$$
(11)

Where,

$$\varepsilon_{nt} = U_n + V_t + w_{nt} \tag{12}$$

If the individual (U_n) and temporal (V_t) effects are random, with a zero mean and variance, σ_u^2 and σ_v^2 . The model is easily decomposed, with the error factor consisting of three elements: a component that does not exhibit autocorrelation (w_{nt}) either individually or temporally, a component as an individual-specific effect (U_n) , and a component as a temporal-specific effect (V_t) , which are not correlated with each other or with each other.

These features give a condition mean value y_{nt} as shown in Equation (13).

$$E(y_{nt}/x_{1nt}, \dots, x_{Knt}) = b_0 + \sum_{k=1}^{K} b_k x_{knt}$$
(13)

Individual effects in the random effect model represent unobservable human characteristics and are uncorrelated with dependent observable variables. F and Hausman tests are used to choose one of two types of models (with fixed or random effects).

2.5. Hausman Tests

The Hausman test is also referred to as a model misspecification test. The Hausman test can help to select between a fixed effects model and a random effects model in panel data analysis (data analysis over time) [11]. The null hypothesis states that the chosen model has random effects, whereas the alternative hypothesis states that the model has fixed effects. The tests essentially try to check if there is a relationship between the unique mistakes and the regressors in the model. The null hypothesis states that no association exists between the two. The interpretation of a Hausman test result is simple: if the p-value is tiny (less than 0.05), reject the null hypothesis.

2.6. Reviewed Works

In carrying out panel data analysis, [14] investigated the impact of bank-specific and macroeconomic major drivers on the profitability of Islamic retail banks in Bahrain. It utilized explanatory research with secondary financial data and utilized panel data from six Islamic retail banks from 2013 to 2019. The two primary profitability measurements employed in this study are Return on Assets (ROA) and Return on Equity (ROE). The two statistical models used in this study are the random effect regression model and the fixed effect regression model.

According to the random effect regression model, bank size is strongly favourably connected to ROA, but operational efficiency and GDP growth have significant and negative relationships with ROA. The fixed effect regression model reveals that credit risk, operating efficiency, and GDP growth rate have negative significant effects on banks' ROE. The study did not predict the future outcome values for ROE and ROA, and the basis for selecting a regression model was not established in the study.

In assessing the performance of the banks in Bangladesh through the efficiency of the banks. Uddin and Nezum [15] used a Z score methodology, where the Z score was also used as the dependent variable. The fraction of total operating expenditures and net operating income of banks is calculated. Other indices are regressed on the Z score. From 2015 to 2017, the panel data estimation approach is employed. In that respect, two models were developed, with model-1 including 6(six) explanatory factors and model-2 containing an extra independent variable in addition to the previous six variables. Two effect models (fixed effect and random effect) are also calculated in the panel data estimation way. The random effect is shown to be appropriate for both models. According to the random effect, [15] discovered that three factors had a negative influence on the Z score in model-1, whereas three variables had a favourable impact. In model-2, three indices have a negative influence on the Z score, whereas four indices have a favourable effect. Surprisingly, the efficiency ratio has a significantly favourable influence on the GDP growth rate in both models. Panel data analysis was used in [16] to examine the condition and dynamics of the financial performance of firms listed on the Bucharest Stock Exchange in relation to determinant variables. The study presented a theoretical foundation as well as an applied panel data analysis of two case studies using fixed and random-effects models (investigating the influence of ROE of the previous period on ROE for the current period). The findings of the Hausman test are used to choose which of the two types of models to use. The outcome of the study in [16] justifies panel analysis of return on equity for monitoring the performance measures of financial organizations.

Other than assessing the performance of banks, panel data analysis was used to discover the profitability factors of the banking sector in [12], where the impact of the determinants of profitability on the commercial banks in Asian countries was the objective study in [12]. To evaluate the data, the panel data research approach was employed as an estimating tool. Data was also examined using the ordinary least squares (OLS) regression model. The Breusch-Pagan Lagrange Multiplier (LM) Test was used to determine whether the models were adequate. Bank-specific and microeconomic parameters varied virtually identically for private banks in Bangladesh and India.

E-views econometric software was used to analyze all models and tests. The study discovers that the Return on Asset (ROA) from the banks' individual factors, Bank Size (BS), and Debt to Asset Ratio (DAR), are positive and substantial. The Deposit to Asset Ratio (DTAR) and Loan to Deposit Ratio (LDR) for banks are shown to be negative and substantial. The Equity to Asset (EAR) and Debt to Equity (DER) ratios have neither positive nor negative influence. But, the study did not apply predictive analytics for future determination. Also, panel data analysis has been used to determine the dividends and performance of firms in India.



Fig. 2 The general process model

3. Methodology

Figure 2 shows the general flow of the developed model. The sourced data was obtained from different sources. The data was cleaned and preprocessed, and the quality check was done to ascertain that the features obtained were complete with no irregularities in the dataset.

The dataset was transformed to panel data having 19 features from 10 Nigerian banks (Union, Sterling, Wema, Access, GT, Zenith, Fidelity, First, FCMB, and UBA banks) over a period of 22 years. The panel data was analyzed using two-panel data analysis models: the random effects and the fixed effects models. The best-performing model was selected based on the Hausman Test, with p values tending more to zero (0).

4. Result and Discussion

The focus is to examine how the Fixed effects and the Random effects models performed in the face of the panel dataset. Although the predicting and predicted factors were not of major concern, the performance of the two models. The Return on Asset (RoA) was used as the performance indicator for the panel dataset.

Figure 3 shows the output of the fixed effects model on the panel dataset. Figure 4 shows the output of the random effects model on the panel data. In developing the two regression models, the least squares dummy variable method was used so as to factor in the variance in the unobserved variables. In doing this, the bank column containing eight (8) variables was converted to 8 dummy variables, and one of these dummy variables was left out so as to avoid perfect Multicollinearity between the 8 dummy variables. The regression model's intercept will hold the value of the coefficient for the left-out dummy variable.

The result of the regression analysis for the fixed effects model showed values for the effects of endogenous and exogenous elements on bank performance (ROA). The coefficient value for the Debt Burden Ratio (DBR) is statistically significant at p < 0.05 with a p-value = 0.025. Also, the bank-specific effects FCMB, FirstBank, GTB, and Wema are statistically significant at a p < 0.01 with p-values = 0.000 each.

We may choose to qualify Board Oversight Function (BOF) to be statistically significant at p < 0.05. This can be attributed to the unobserved behaviour of the variable within the model. The remaining predictors are all statistically insignificant at p-value < 0.05, as indicated in the p > |t| column.

The outcome of the random effects model, as depicted in Figure 3, only indicates that only Debt Burden Ratio (DBR) coefficient is statistically significant at p < 0.05 with the pvalue = 0.022.

		Fixe	d Effects M	odel ======		
		OLS Reg	ression Res	ults		
Dep. Variabi	le:	n	oa R-squa	red:		0.669
Model:		0	LS Adj. R	-squared:		0.600
Method:		Least Squar	es F-stat	istic:		9.663
Date:	Mo	n, 20 Mar 20	23 Prob (F-statistic):	1.35e-16
Time:		02:00:	01 Log-Li	kelihood:		97.156
No. Observat	tions:	1	28 AIC:			-148.3
Of Residuals	5:	1	05 BIC:			-82.72
Df Model:			22			
Covariance 1	Type:	nonrobu	st			
	coef	std err	t	P> t	[0.025	0.975]
Intercent	-0 3810	A 262	-1 454	Ø 149	-0 901	A 139
Ide	0.3010	0.202	0 963	0.145	-0.301	0.155
the	0.0700	0.001	2 292	0.000	0.102	0.200
101	0.1500	0.007	2.202	0.025	0.020	0.576
ur nef	-0.0493	0.128	-0.384	0.702	-0.303	0.205
ост	0.2/02	0.149	1.81/	0.0/2	-0.025	0.565
og	0.1633	0.086	1.896	0.061	-0.008	0.334
ar	0.1952	0.1/3	1.129	0.262	-0.148	0.538
ecs	0.0557	0.155	0.359	0.720	-0.251	0.363
rm	-0.1241	0.164	-0.758	0.450	-0.449	0.201
LS	0.1206	0.094	1.285	0.202	-0.065	0.30/
cas	0.0611	0.088	0.694	0.489	-0.114	0.236
aq	0.0139	0.159	0.088	0.930	-0.301	0.329
pof	0.1920	0.100	1.915	0.058	-0.007	0.391
ta	0.0944	0.097	0.971	0.334	-0.098	0.287
infl	-0.0404	0.068	-0.598	0.551	-0.174	0.094
gdp	-0.0960	0.057	-1.684	0.095	-0.209	0.017
Acess	0.0802	0.051	1.566	0.120	-0.021	0.182
<pre>FCMB</pre>	0.4842	0.061	7.935	0.000	0.363	0.605
Fidelity	0.1760	0.054	3.280	0.001	0.070	0.282
FirstBank	0.2729	0.066	4.118	0.000	0.142	0.404
STB	0.1811	0.050	3.610	0.000	0.082	0.281
JBA	0.1108	0.061	1.818	0.072	-0.010	0.232
Vema	0.4407	0.057	7.736	0.000	0.328	0.554
omnibus:		5 9	95 Durbin	-Watson:		1.241
Prob(Omnibus):		 	71 Jacque	-Bera (JR)	4,891	
Cham.		0.0	76 Prob(1	roh(IB):		0 0867
Vurtosis:		0.5	92 Cond	No.		6.000/
Vui C0315.		5.5	ss conu.			02.4

Notes:

Notes: [1] Standard Errors assume that the covariance matrix of the errors is correctly specified. sigma2_epsilon = 0.03569319800343661 sigma2_u = 0.019902048530155026 theta = 0.7826357564864186

Fig. 3 The outcome of the fixed effects model

Random Effects Model								
OLS Regression Results								
Dep. Variał	ble:	r	oa R-squa	red:		0.280		
Model:		0)LS Adj.R	-squared:		0.184		
Method:		Least Squar	es F-stat	istic:		2.909		
Date:	MOI	n, 20 Mar 20	23 Prob (F-statistic)	: · · · · · · · · · · · · · · · · · · ·	0.000662		
Time:		02:04:	42 Log-Li	kelihood:		91.524		
No. Observa	ations:	1	28 AIC:			-151.0		
Df Residual	ls:	1	12 BIC:			-105.4		
Df Model:			15					
Covariance	Type:	nonrobu	ist					
	coef	std err	t	P> t	[0.025	0.975]		
const	-0.1031	0.253	-0.408	0.684	-0.605	0.398		
ldr	0.0753	0.090	0.835	0.406	-0.103	0.254		
dbr	0.2031	0.087	2.329	0.022	0.030	0.376		
cn	-0.0301	0.129	-0.233	0.816	-0.286	0.226		
ocf	0.2580	0.150	1.719	0.088	-0.039	0.556		
bg	0.1586	0.087	1.823	0.071	-0.014	0.331		
car	0.1437	0.173	0.830	0.408	-0.199	0.486		
ecs	0.0630	0.156	0.403	0.688	-0.247	0.373		
crm	-0.1344	0.163	-0.822	0.413	-0.458	0.189		
15	0.1153	0.093	1,239	0.218	-0.069	0.300		
cas	0.0479	0.089	0.541	0.589	-0.127	0.223		
ag	0.0051	0.160	0.032	0.974	-0.312	0.322		
bof	0.1724	0.098	1.765	0.080	-0.021	0.366		
ta	0.0666	0.097	0.684	0.495	-0.126	0.260		
infl	-0.0316	0.068	-0.465	0.642	-0.166	0.103		
gdn	-0 1002	0.057	-1 743	0 084	-0 214	0.105		
54P	-0.1002		-11/45		-0.214			
Omnihus: 14,159 Durbin-Watson: 1,658								
Prob(Omnibu	us):	A 4	01 Jacque	-Bera (JB)		16.836		
Skew		0.0	77 Proh(1	R).		0 000221		
Kurtosis:		4.1	51 Cond.	No.		13.4		
			Cond.			13.7		

Notes: [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Fig. 4 The outcome of the random effects model

This becomes a challenge in deciding on the model to choose. Therefore, there is a need to choose a better model between the Random effects and Fixed effects models that actually model the choice of panel data accurately. Therefore, the study adopted the Hausman Test to help make a decision on a better model through the hypothesis testing as shown;

H₀: The Random Effects model is the preferred model for panel data analysis

 H_1 : The fixed effects Model is the preferred model.

In determining the most appropriate estimating approach, the study carried out a Hausman test to decide whether to use the Fixed Effect (FE) or Random Effect (RE) Model. The outcome of the Hausman test is shown in Figure 5. Judging by the p-value of 4.4310667577614615e-17, which is very close to 0.00, we reject the null hypothesis (random effect) and accept the use of the fixed effect analysis as there is a correlation between the unique errors and the regressors in the model.

Hausman Test

chi-Squared: 24.452667918156116 degrees of freedom: 16 p-Value: 4.4310667577614615e-17

Ratio	Full Name	Co-	
		efficient	
Intercept		-0.3810	
LDR	Loan Deposit Ratio	0.0788	
DBR	Debt Burden Ratio	0.1980	
CR	Current Ratio	-0.0493	
OCF	Operating Cashflow	0.2702	
BG	Bank Growth	0.1633	
CAR	Capital Adequacy	0.1952	
	Ratio		
ECS	Equity Capital	0.0557	
	Structure		
CRM	Credit Risk	0.1244	
	Management		
LS	Loan Structure	0.1206	
CAS	Cash Asset	0.0611	
	Structure		
AQ	Accrual Quality	0.0139	
TA	Total Asset	0.0944	
BOF	Board Oversight	0.1920	
	Function		
INFL	Inflation	-0.0404	
GDP	GDP Gross Domestic		
	Product		

Table 1. Co-efficient values for the predicting variables

The result of the Fixed effects model is thoroughly explained in this section. Table 1 shows the summary of the co-efficient values for the exogenous or predicting variable.

In Table 1, the coefficient values of the exogenous variables have a direct influence on the targeted variable, ROA. The positive values indicate that as the values increase, the effect on ROA also increases, unlike the negative value coefficients, which cause a reduction effect on ROA.

4.1. Goodness-of-fit Evaluation Metrics

Aside the coefficients and the p values, the goodness-offit of the Fixed Effects Model (FEM) needs to be analyzed. The goodness-of-fit measures how well the fixed effects model fits the given collection of panel data. This can be placed on the check by first looking at the following;

The Adjusted R-Squared value, which yielded 0.600 from the FEM results in Fig. 3, where;

R-Squared = 0.669 Adj. R-Squared = 0.600

After accounting for the degrees of freedom lost owing to the existence of regression variables, the adjusted R-squared reflects the proportion of the variation in the response variable ROA that the model was able to explain. The adjusted Rsquared of 0.600 (or around 60%) indicates a good fit despite the unobserved variables.

The F-statistics for a fixed effects regression model analysis determines if all model coefficients are jointly significant and, hence, whether the FE model has a good goodness-of-fit. It can be observed that the F-test value of 9.663 is significant at p<.001, showing that the model's goodness-of-fit is correct. This is evident in the FEM result shown in Figure 4, where;

F-statistic = 9.663 Prob (F-statistic) = 1.35e-16

The Meaningless values (Log-likelihood and Akaike Information Criterion (AIC)) are the values used for measuring a model fit that may be used to compare different types of models (or variations on the same model). Higher values indicate a better model fit. The log-likelihood and AIC are accessible from the FEM results in Figure 3, where,

Log-likelihood = 97.156

4.2. Generated Panel Data Regression Equation

The coefficient of the variables obtained from this study can be fitted into the panel data model given in equation 8.

$$Y_{it} = \beta_0 + \beta_1 x \mathbf{1}_{it} + \beta_2 x \mathbf{2}_{it} + \beta_3 x \mathbf{3}_{it} + \dots + \beta_n x n_{it} *$$

$$\varepsilon_{it}$$
(14)

Where Y_{it} is the dependent variable,

 $x1 \dots xn$ represent the number of predicting variables, $\beta_0 \dots \beta_n$ are the coefficients of the predicting variables, and *it* is the change in the group being observed over time t. By substituting these variables with the variables used in this study, equation 15 was obtained

$$ROA_{it} = \beta_0 + \beta_1 ldr_{it} + \beta_2 dbr_{it} + \beta_3 ocf_{it} + \cdots + \beta_n gdp_{it} * \varepsilon_{it}$$
(15)

Then, substitute the actual coefficient values from Table 1 to obtain equation 16. Equation 9 becomes the panel data regression model.

 $ROA_{it} = -0.3810 + (0.0788)ldr_{it} + (0.1980)dbr_{it} + (-0.0493)ocf_{it} + \dots + (-0.0960)gdp_{it} * \varepsilon_{it}$ (16)

4.3. Fixed Effects Panel Data Model Benchmark Evaluation

The outcome of the panel data fixed effects model was benchmarked with other models by fitting the models on the panel data. The benchmark was measured using the goodnessof-fit metrics (Adjusted R-squared, F-statistic, Log-likelihood and AIC). The outcome, as evident in Table 2, shows that the panel data fixed effects model has the best good-of-fit values. The competing models are the pooled OLS panel data model used in [11] and the Fixed effects panel data model used in [13].

Table 2. Benchmarking the Fixed Effects model against Pooled OLS and Random Effects panel data Models

Models	Adj. R- squared (%)	F-statistic (%)	Log-likelihood	AIC
Random Effects	0.184	2.909	91.524	-151.0
Fixed Effects	0.600	0.033	97.156	-148.3

5. Summary

In summary, the above results imply that all the variables jointly affect ROA performance. Also, the value of the adjusted coefficient of multiple determination of 0.600 means that the combined changes in the exogenous and endogenous variables would cause 60% changes in ROA while the remaining changes of 40% per cent are caused by other factors which are not within the coverage of the model. These variables are referred to as the unobserved variables. The adjusted R-squared is a modified version of the R-squared that adjusts for the number of predictors in the regression model. The Hausman test with the Chi-square value of 24.45 and the p-value of 4.4310667577614615e-17, which is less than the 5% chosen significant level (p<.05), shows that the null hypothesis is therefore rejected. Accept the alternate hypothesis and conclude that the Fixed Effects model is suitable for the panel data analysis with exogenous and endogenous variables affecting bank ROA among deposit money banks in Nigeria.

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